

THE  
CABINET CYCLOPÆDIA.



LONDON :  
Printed by A. & R. Spottiswoode,  
New-Street-Square.

THE  
CABINET CYCLOPÆDIA.

CONDUCTED BY THE  
REV. DIONYSIUS LARDNER, LL.D. F.R.S. L. & E.  
M.R.I.A. F.L.S. F.Z.S. Hon. F.C.P.S. M.Ast.S. &c. &c.

ASSISTED BY  
EMINENT LITERARY AND SCIENTIFIC MEN.

---

Natural Philosophy.

---

MECHANICS.

BY  
CAPTAIN HENRY KATER, V.Pres.R.S. &c.  
AND THE  
REV. DIONYSIUS LARDNER, LL.D. F.R.S. &c.

---

LONDON:

PRINTED FOR  
LONGMAN, REES, ORME, BROWN, AND GREEN,  
PATERNOSTER-ROW;  
AND JOHN TAYLOR,  
UPPER GOWER STREET.

1830.

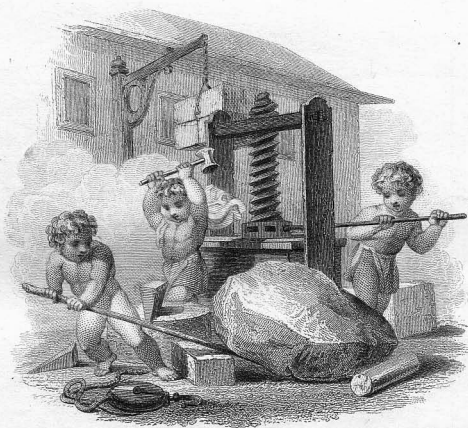
A  
TREATISE ON MECHANICS,

by

CAPTAIN HENRY KATER, V. PRES: R. S.

and

REV: DIONYSIUS LARDNER, L.L.D. F.R.S. L & E.



*H. Corbould del.*

*E. Finden sc.*

London:

PRINTED FOR LONGMAN, REES, ORME, BROWN & GREEN, PATERNOSTER ROW.  
AND JOHN TAYLOR, UPPER GOWER STREET.

1830.

## ADVERTISEMENT.

---

THIS Treatise being the joint production of two persons, it is right to state the portions of it which are the exclusive work of each. The chapter on Balances and Pendulums, the instruments on which the measurement of *weight* and *time* depends, has been written by Captain Kater. For the remainder of the volume, Dr. Lardner is responsible.

# CONTENTS.

---

## CHAP. I.

### PROPERTIES OF MATTER.

Organs of Sense — Sensations. — Properties or Qualities. — Observation. — Comparison and Generalisation. — Particular and general Qualities. — Magnitude. — Size. — Volume. — Lines. — Surfaces. — Edges. — Area. — Length. — Impenetrability. — Apparent Penetration. — Figure. — Different from Volume. — Atoms. — Molecules. — Matter separable. — Particles. — Force. — Cohesion of Atoms. — Hypothetical Phrases unnecessary. — Attraction. - - - - - Page 1

## CHAP. II.

### PROPERTIES OF MATTER, CONTINUED.

Divisibility. — Unlimited Divisibility. — Wollaston's micrometric Wire. — Method of making it. — Thickness of a Soap Bubble. — Wings of Insects. — Gilding of Embroidery. — Globules of the Blood. — Animalcules. — Their minute Organisation. — Ultimate Atoms. — Crystals. — Porosity. — Volume. — Density. — Quicksilver passing through Pores of Wood. — Filtration. — Porosity of Hydrophane. — Compressibility. — Elasticity. — Dilatability. — Heat. — Contraction of Metal used to restore the Perpendicular to Walls of a Building. — Impenetrability of Air. — Compressibility of it. — Elasticity of it. — Liquids not absolutely incompressible. — Experiments. — Elasticity of Fluids. — Aeriform Fluids. — Domestic Fire Box. — Evolution of Heat by compressed Air. - - - - - 9

## CHAP. III.

### INERTIA.

Inertia. — Matter incapable of spontaneous Change. — Impediments to Motion. — Motion of the Solar System. — Law of Nature. — Spontaneous Motion. — Immateriality of the thinking and willing Principles. — Language used to express Inertia sometimes faulty. — Familiar Examples of Inertia. - - - - - 27

## CHAP. IV.

### ACTION AND REACTION.

Inertia in a single Body. — Consequences of Inertia in two or more Bodies. — Examples. — Effects of Impact. — Motion not estimated by Speed or Velocity alone. — Examples. — Rule for estimating the Quantity of Motion. — Action and Reaction. — Examples of. — Velocity of two Bodies after Impact. — Magnet and Iron. — Feather and Cannon Ball impinging. — Newton's Laws of Motion. — Inutility of. - - - - - 35

## CHAP. V.

## COMPOSITION AND RESOLUTION OF FORCE.

Motion and Pressure. — Force. — Attraction. — Parallelogram of Forces. — Resultant. — Components. — Composition of Force. — Resolution of Force. — Illustrative Experiments. — Composition of Pressures. — Theorems regulating Pressures also regulate Motion. — Examples. — Resolution of Motion. — Forces in Equilibrium. — Composition of Motion and Pressure. — Illustrations. — Boat in a Current. — Motions of Fishes — Flight of Birds. — Sails of a Vessel. — Tacking. — Equestrian Feats. — Absolute and relative Motion. - - - - - Page 48

## CHAP. VI.

## ATTRACTION.

Impulse. — Mechanical State of Bodies. — Absolute Rest. — Uniform and rectilinear Motion. — Attractions. — Molecular or atomic. — Interstitial Spaces in Bodies. — Repulsion and Attraction. — Cohesion. — In Solids and Fluids. — Manufacture of Shot. — Capillary Attractions. — Shortening of Rope by Moisture. — Suspension of Liquids in capillary Tubes. — Capillary Siphon. — Affinity between Quicksilver and Gold. — Examples of Affinity. — Sulphuric Acid and Water. — Oxygen and Hydrogen. — Oxygen and Quicksilver. — Magnetism. — Electricity and Electro-Magnetism. — Gravitation. — Its Law. — Examples of. — Depends on the Mass. — Attraction between the Earth and detached Bodies on its Surface. — Weight. — Gravitation of the Earth. — Illustrated by Projectiles. — Plumb-Line. — Cavendish's Experiments. - - - 63

## CHAP. VII.

## TERRESTRIAL GRAVITY.

Phenomena of falling Bodies. — Gravity greater at the Poles than Equator. — Heavy and light Bodies fall with equal Speed to the Earth. — Experiment. — Increased Velocity of falling Bodies. — Principles of uniformly accelerated Motion. — Relations between the Height, Time, and Velocity. — Attwood's Machine. — Retarded Motion. - - - 82

## CHAP. VIII.

## OF THE MOTION OF BODIES ON INCLINED PLANES AND CURVES.

Force perpendicular to a Plane. — Oblique Force. — Inclined Plane. — Weight produces Pressure and Motion. — Motion uniformly accelerated. — Space moved through in a given Time. — Increased Elevation produces increased Force. — Perpendicular and horizontal Plane. — Final Velocity. — Motion down a Curve. — Depends upon Velocity and Curvature. — Centrifugal Force. — Circle of Curvature. — Radius of Curvature. — Whirling Table. — Experiments. — Solar System. — Examples of centrifugal Force. - - - - - 93

## CHAP. IX.

## THE CENTRE OF GRAVITY.

Terrestrial Attraction the combined Action of parallel Forces. — Single equivalent Force. — Examples. — Method of finding the Centre of Gra-

vity. — Line of Direction. — Globe. — Oblate Spheroid. — Prolate Spheroid. — Cube. — Straight Wand. — Flat Plate. — Triangular Plate. — Centre of Gravity not always within the Body. — A Ring. — Experiments. — Stable, instable, and neutral Equilibrium. — Motion and Position of the Arms and Feet. — Effect of the Knee-Joint. — Positions of a Dancer. — Porter under a Load. — Motion of a Quadruped. — Rope Dancing. — Centre of Gravity of two Bodies separated from each other. — Mathematical and experimental Examples. — The Conservation of the Motion of the Centre of Gravity. — Solar System. — Centre of Gravity sometimes called Centre of Inertia - - - Page 107

## CHAP. X.

## THE MECHANICAL PROPERTIES OF AN AXIS.

An Axis. — Planets and common spinning Top. — Oscillation or Vibration. — Instantaneous and continued Forces. — Percussion. — Continued Force. — Rotation. — Impressed Forces. — Properties of a fixed Axis difficult. — Movement of the Force round the Axis. — Leverage of the Force. — Impulse perpendicular to, but not crossing, the Axis. — Radius of Gyration. — Centre of Gyration. — Moment of Inertia. — Principal Axes. — Centre of Percussion - - - - - 128

## CHAP. XI.

## OF THE PENDULUM.

Isochronism. — Experiments. — Simple Pendulum. — Examples illustrative of. — Length of. — Experiments of Kater, Biot, Sabine, and others. — Huygen's Cycloidal Pendulum - - - - - 145

## CHAP. XII.

## OF SIMPLE MACHINES.

Statics. — Dynamics. — Force. — Power. — Weight. — Lever. — Cord. — Inclined Plane - - - - - 160

## CHAP. XIII.

## OF THE LEVER.

Arms. — Fulcrum. — Three Kinds of Levers. — Crow Bar. — Handspike. — Oar. — Nutcrackers. — Turning Lathe. — Steelyard. — Rectangular Lever. — Hammer. — Load between two Bearers. — Combination of Levers. — Equivalent Lever - - - - - 167

## CHAP. XIV.

## OF WHEEL-WORK.

Wheel and Axle. — Thickness of the Rope. — Ways of applying the Power. — Projecting Pins. — Windlass. — Winch. — Axle. — Horizontal Wheel. — Tread-Mill. — Cranes. — Water-Wheels. — Paddle-Wheel. — Ratchet-Wheel. — Rack. — Spring of a Watch. — Fusee. — Straps or Cords. — Examples of. — Turning Lathe. — Revolving Shafts. — Spinning Machinery. — Saw-Mill. — Pinion. — Leaves. — Crane. — Spur-Wheels. — Crown-Wheels. — Bevelled Wheels. — Hunting-Cog. — Chronometers — Hair-Spring. — Balance-Wheel - - - - - 178



## CHAP. XV.

## OF THE PULLEY.

Cord. — Sheave. — Fixed Pulley. — Fire Escapes. — Single moveable Pulley. — Systems of Pulleys. — Smeaton's Tackle. — White's Pulley. — Advantage of. — Runner. — Spanish Bartons - - Page 199

## CHAP. XVI.

## ON THE INCLINED PLANE, WEDGE, AND SCREW.

Inclined Plane. — Effect of a Weight on. — Power of. — Roads. — Power Oblique to the Plane. — Plane sometimes moves under the Weight. — Wedge. — Sometimes formed of two inclined Planes. — More powerful as its Angle is acute. — Where used. — Limits to the Angle. — Screw. — Hunter's Screw. — Examples. — Micrometer Screw - - 209

## CHAP. XVII.

## ON THE REGULATION AND ACCUMULATION OF FORCE.

Uniformity of Operation. — Irregularity of prime Mover. — Water-Mill. — Wind-Mill. — Steam Pressure. — Animal Power. — Spring. — Regulators. — Steam-Engine. — Governor. — Self-acting Damper. — Tachometer. — Accumulation of Power. — Examples. — Hammer. — Flail. — Bow-string. — Fire Arms. — Air-Gun. — Steam-Gun. — Inert Matter a Magazine for Force. — Fly-Wheel. — Condensed Air. — Rolling Metal. — Coining-Press - - - - 224

## CHAP. XVIII.

## MECHANICAL CONTRIVANCES FOR MODIFYING MOTION.

Division of Motion into rectilinear and rotatory. — Continued and reciprocating. — Examples. — Flowing Water. — Wind. — Animal Motion. — Falling of a Body. — Syringe-Pump. — Hammer. — Steam-Engine. — Fulling Mill. — Rose-Engine. — Apparatus of Zureda. — Leupold's Application of it. — Hooke's universal Joint. — Circular and alternate Motion. — Examples. — Watt's Methods of connecting the Motion of the Piston with that of the Beam. — Parallel Motion - - - - 245

## CHAP. XIX.

## OF FRICTION AND THE RIGIDITY OF CORDAGE.

Friction and Rigidity. — Laws of Friction. — Rigidity of Cordage. — Strength of Materials. — Resistance from Friction. — Independent of the Magnitude of Surfaces. — Examples. — Vince's Experiments. — Effect of Velocity. — Means for diminishing Friction. — Friction Wheels. — Angle of Repose. — Best Angle of Draught. — Rail-Roads. — Stiffness of Ropes 260

## CHAP. XX.

## ON THE STRENGTH OF MATERIALS.

Difficulty of determining the Laws which govern the Strength of Materials. — Forces tending to separate the Parts of a Solid. — Laws by which

Solids resist Compression. — Euler's theory. — Transverse Strength of Solids. — Strength diminished by the Increase of Height. — Lateral or Transverse Strain. — Limits of Magnitude. — Relative Strength of small Animals greater than large ones - - - Page 272

## CHAP. XXI.

## ON BALANCES AND PENDULUMS.

Weight. — Time. — The Balance. — Fulcrum. — Centre of Gravity of. — Sensibility of. — Positions of the Fulcrum. — Beam variously constructed. Troughton's Balance. — Robinson's Balance. — Kater's Balance. — Method of adjusting a Balance. — Use of it. — Precautions necessary. — Of Weights. — Adjustment of. — Dr. Black's Balance. — Steelyard. — Roman Statera or Steelyard. — Convenience of. — C. Paul's Steelyard. — Chinese Steelyard. — Danish Balance. — Bent Lever Balance. — Brady's Balance. — Weighing Machine for Turnpike Roads. — Instruments for Weighing by means of a Spring. — Spring Steelyard. — Salter's Spring Balance. — Marriott's Dial Weighing Machine. — Dynamometer. — Compensation Pendulums. — Barton's Gridiron Pendulum. — Table of linear Expansion. — Second Table. — Harrison's Pendulum. — Troughton's Pendulum. — Benzenberg's Pendulum. — Ward's Compensation Pendulum. — Compensation Tube of Julien le Roy. — Deparcieux's Compensation. — Kater's Pendulum. — Reed's Pendulum. — Ellicott's Pendulum. — Mercurial Pendulum. — Graham's Pendulum. — Compensation Pendulum of Wood and Lead. — Smeaton's Pendulum. — Brown's Mode of Adjustment.

# THE ELEMENTS OF MECHANICS.

---

## CHAP. I.

PROPERTIES OF MATTER — MAGNITUDE — IMPENETRABILITY — FIGURE — FORCE.

(1.) **P**LACED in the material world, Man is continually exposed to the action of an infinite variety of objects by which he is surrounded. The body, to which the thinking and living principles have been united, is an apparatus exquisitely contrived to receive and to transmit these impressions. Its various parts are organised with obvious reference to the several external agents by which it is to be affected. Each organ is designed to convey to the mind immediate notice of some peculiar action, and is accordingly endued with a corresponding susceptibility. This adaptation of the organs of sense to the particular influences of material agents, is rendered still more conspicuous when we consider that, however delicate its structure, each organ is wholly insensible to every influence except that to which it appears to be specially appropriated. The eye, so intensely susceptible of impressions from light, is not at all affected by those of sound ; while the fine mechanism of the ear, so sensitively alive to every effect of the latter class, is altogether insensible to the former. The splendour of excessive light may occasion blindness, and deafness may result from the roar of a cannonade ; but neither the sight nor the hearing can be injured by the most ex-

treme action of that principle which is designed to affect the other.

Thus the organs of sense are instruments by which the mind is enabled to determine the existence and the qualities of external things. The effects which these objects produce upon the mind through the organs, are called *sensations*, and these sensations are the immediate elements of all human knowledge. *MATTER* is the general name which has been given to that substance, which, under forms infinitely various, affects the senses. Metaphysicians have differed in defining this principle. Some have even doubted of its existence. But these discussions are beyond the sphere of mechanical philosophy, the conclusions of which are in nowise affected by them. Our investigations here relate, not to matter as an abstract existence, but to those qualities which we discover in it by the senses, and of the existence of which we are sure, however the question as to matter itself may be decided. When we speak of "bodies," we mean those things, whatever they be, which excite in our minds certain sensations; and the powers to excite those sensations are called "properties," or "qualities."

(2.) To ascertain by observation the properties of bodies, is the first step towards obtaining a knowledge of nature. Hence man becomes a natural philosopher the moment he begins to feel and to perceive. The first stage of life is a state of constant and curious excitement. Observation and attention, ever awake, are engaged upon a succession of objects new and wonderful. The large repository of the memory is opened, and every hour pours into it unbounded stores of natural facts and appearances, the rich materials of future knowledge. The keen appetite for discovery implanted in the mind for the highest ends, continually stimulated by the presence of what is novel, renders torpid every other faculty, and the powers of reflection and comparison are lost in the incessant activity and unexhausted vigour of observation. After a season, however, the

more ordinary classes of phenomena cease to excite by their novelty. Attention is drawn from the discovery of what is new, to the examination of what is familiar. From the external world the mind turns in upon itself, and the feverish astonishment of childhood gives place to the more calm contemplation of incipient maturity. The vast and heterogeneous mass of phenomena collected by past experience is brought under review. The great work of comparison begins. Memory produces her stores, and reason arranges them. Then succeed those first attempts at generalisation which mark the dawn of science in the mind.

To compare, to classify, to generalise, seem to be instinctive propensities peculiar to man. They separate him from inferior animals by a wide chasm. It is to these powers that all the higher mental attributes may be traced, and it is from their right application that all progress in science must arise. Without these powers, the phenomena of nature would continue a confused heap of crude facts, with which the memory might be loaded, but from which the intellect would derive no advantage. Comparison and generalisation are the great digestive organs of the mind, by which only nutrition can be extracted from this mass of intellectual food, and without which, observation the most extensive, and attention the most unremitting, can be productive of no real or useful advancement in knowledge.

(3.) Upon reviewing those properties of bodies which the senses most frequently present to us, we observe that very few of them are essential to, and inseparable from, matter. The greater number may be called *particular* or *peculiar qualities*, being found in some bodies but not in others. Thus the property of attracting iron is peculiar to the loadstone, and not observable in other substances. One body excites the sensation of green, another of red, and a third is deprived of all colour. A few characteristic and essential qualities are, however, inseparable from matter in whatever state, or

under whatever form it exist. Such properties alone can be considered as tests of materiality. Where their presence is neither manifest to sense, nor demonstrable by reason, *there matter is not*. The principal of these qualities are *magnitude* and *impenetrability*.

(4.) *Magnitude*.—Every body occupies space, that is, it has magnitude. This is a property observable by the senses in all bodies which are not so minute as to elude them, and which the understanding can trace to the smallest particle of matter. It is impossible, by any stretch of imagination, even to conceive a portion of matter so minute as to have no magnitude.

The *quantity* of space which a body occupies is sometimes called its *magnitude*. In colloquial phraseology, the word *size* is used to express this notion; but the most correct term, and that which we shall generally adopt is *volume*. Thus we say, the volume of the earth is so many cubic miles, the volume of this room is so many cubic feet.

The external limits of the magnitude of a body are *lines* and *surfaces*, lines being the limits which separate the several surfaces of the same body. The linear limits of a body are also called *edges*. Thus the line which separates the top of a chest from one of its sides is called an edge.

The *quantity* of a surface is called its *area*, and the *quantity* of a line is called its *length*. Thus we say, the *area* of a field is so many acres, the *length* of a rope is so many yards. The word “magnitude” is, however, often used indifferently for volume, area, and length. If the objects of investigation were of a more complex and subtle character, as in metaphysics, this unsteady application of terms might be productive of confusion, and even of error; but in this science the meaning of the term is evident, from the way in which it is applied, and no inconvenience is found to arise.

(5.) *Impenetrability*.—This property will be most clearly explained by defining the positive quality from which it takes its name, and of which it merely signifies

the absence. A substance would be *penetrable* if it were such as to allow another to pass through the space which it occupies, without disturbing its component parts. Thus, if a comet striking the earth could enter it at one side, and, passing through it, emerge from the other without separating or deranging any bodies on or within the earth, then the earth would be penetrable by the comet. When bodies are said to be impenetrable, it is therefore meant that one cannot pass through another without displacing some or all of the component parts of that other. There are many instances of apparent penetration; but in all these, the parts of the body which seem to be penetrated are displaced. Thus, if the point of a needle be plunged in a vessel of water, all the water which previously filled the space into which the needle enters will be displaced, and the level of the water will rise in the vessel to the same height as it would by pouring in so much more water as would fill the space occupied by the needle.

(6.) *Figure*. — If the hand be placed upon a solid body, we become sensible of its impenetrability, by the obstruction which it opposes to the entrance of the hand within its dimensions. We are also sensible that this obstruction commences at certain places; that it has certain determinate limits; that these limitations are placed in certain directions relatively to each other. The mutual relation which is found to subsist between these boundaries of a body, gives us the notion of its *figure*. The *figure* and *volume* of a body should be carefully distinguished. Each is entirely independent of the other. Bodies having very different *volumes* may have the same *figure*; and in like manner bodies differing in *figure* may have the same *volume*. The figure of a body is what in popular language is called its *shape* or *form*. The volume of a body is that which is commonly called its *size*. It will hence be easily understood, that one body (a globe, for example) may have ten times the volume of another (globe), and yet have the same figure; and that two bodies (as a die and a globe) may have *figures* altogether